

B.Sc. Part II

Paper IV

Current electricity

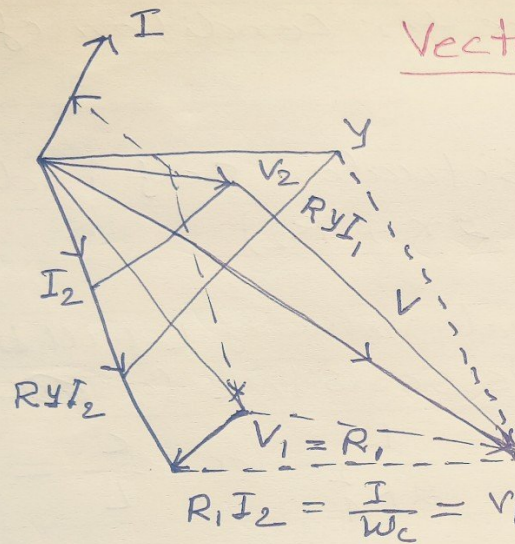
Paper IV

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Current electricity.

Vector Diagram



Since the potential at points E and D of the bridge are equal. Therefore the same current I flows through the capacitor C and resistance r . Hence a voltage $I r$ is developed on the resistance r . Since the current I through

Capacitor C leads the voltage V_3 by phase angle $\pi/2$. The voltage V_1 is equal to the vector sum of $V_3 = \frac{1}{\omega C}$ and $I_2 R$.

Due to equal potential at E and D the voltage $V_3 = R_3 I_2$ and $1/\omega C$ are equal.

The voltage $I_2 R_3$ and current I_2 are in same phase. Also the voltage $R_4 I_2$ and I_2 are in same phase. The voltage $L \omega I_2$ across L lags the current I_2 by phase angle $\pi/2$. The voltage V_4 is equal to the vector sum of $L \omega I_2$ and $R_4 I_2$. I_3 is equal to vector ~~sum~~ sum of I and I_1 .

Voltage V_1 is equal to vector sum of V_1 and V_2 and V_4 also.

Now from the geometry of figure.

$$V_1 = V_{AB} = R_1 I_1 = rI - \frac{I}{j\omega C} I$$

or

$$I = \frac{r + \frac{I}{j\omega C}}{R} I \quad \text{--- (1)}$$

which is equation 1

$$I_1 = \frac{\left(r + \frac{I}{j\omega C}\right) I}{R_1} = 0$$

Again $V_3 = R_3 I_2 = -j \frac{1}{\omega C} I$

or

$$I_3 = \frac{I}{j\omega C R_3} \quad \text{--- (2)}$$

which is equation 2

$$I_2 = \frac{I}{j\omega C R_3}$$

and $V_2 + V_4 = R_2 I_3 + [-(R_4 + j\omega L) I_2]$
 $= V_3 E = (-rI)$

Keeping in view that $V_E > V_B > V_C$ and $V_D = V_E$
from which $V_D = V_C$ we see that

$$V_B - V_C = V_2 = R_2 I_3$$

and

$$V_C - V_D = -(V_D - V_C) = -V_4 = -(R_4 + j\omega L) I_2$$

$$\therefore V_B - V_D = (V_B - V_C) + (V_C - V_D)$$
$$= R_2 I_3 - (R_4 + j\omega L) I_2$$

Again,

$$V_B - V_D = V_B - V_E = (V_E - V_B) = I_r$$

$$\therefore R_2 I_3 - (R_4 + j\omega L) I_2 = -I_r$$

$$\text{or } R_2 I_3 - (R_4 + j\omega L) I_2 = 0 \quad \text{--- (3)}$$

Which is equation

$$R_2 (I_1 + I) - (j\omega L + R_4) I_2 + I_r = 0$$

We have seen that from equation (1) (2) and (3) the condition of balance is

$$L = CR_3 \left[r \left(1 + \frac{R_2}{R_1} \right) + R_2 \right] \text{ and}$$

$$\frac{R_1}{R_2} = \frac{R_3}{R_4}$$